

Original Article

Machine Learning-Based Quantum Circuit Optimization for Noise Reduction

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Abstract

Quantum computing has the potential to revolutionize modern computation and solve problems that classical computing systems are unable of solving, at least within a reasonable time frame. Nevertheless, for current quantum hardware whose performance and reliability are heavily impacted by noise. The subject of this research is the use of machine learning algorithms with quantum circuits to alleviate noise and enhance computational fidelity. Using data-driven models, the proposed method detects patterns of quantum errors and adjusts circuit structures, gate sequences, and qubit mappings accordingly. These include supervised, reinforcement, and deep learning techniques in improving circuit accuracy as well as error rates. It proposes a hybrid optimization framework that combines classical ML algorithms with quantum execution and provides feedback mechanisms for continuous sampling of improved performance. Experimental results show that the fidelity of the optimized circuits and their noise, measured by average gate-fidelity is significantly better than a new set of heuristic methods based on machine learning. The research also covers important topics such as small training data, hardware limitations and scalability. The results are indicative of the essential role that intelligent optimization will play in further developing noise-resilient quantum computing systems and hastening the transition to realistic, scalable quantum applications.

Keywords

Quantum Computing, Quantum Circuit Optimization, Noise Reduction, Machine Learning Reinforcement Learning, Mitigation Of Depolarizing Noise for NISQ Systems

Introduction

Quantum computing is possible to be one of the most disruptive technology innovation in this 21st century, and allows quantum systems to tackle computational problems beyond classical computer. Quantum computing utilizes quantum mechanical principles like superposition, entanglement, and quantum interference to process information in qualitatively different ways. This quality in particular incurs exponential speedups for many classes of problems including things like optimization, cryptography, quantum simulation. Yet, for all its potential, it is obvious that implementing quantum computing will prove difficult — one major challenge being noise in a quantum system.

In the context of quantum computers, noise refers to undesired disturbances that influence the state of a qubit during computation. In contrast to classical systems, where redundancy and error-correcting methods can often repair errors, quantum systems react exceedingly vulnerable to any interaction with the environment. Any small perturbation — be it thermal noise, electromagnetic radiation or an imperfect operation of the gate itself, lead to decoherence and premature collapse of the quantum state. This provides incorrect outputs, and limits the range of quantum computations. This is where current quantum devices sit, known as the Noisy Intermediate-Scale Quantum (NISQ) regime with small numbers of qubits and high error-rates.

Because of these challenges, research direction in noise-aware quantum computing turns into a vital course. This method emphasises the development of noise-immune quantum algorithms and circuits that can deliver their results reliably even if the hardware has limitations. Rather than fighting to nullify noise—which continues to be a long-term goal—noise-aware techniques can reduce its impact with carefully thought-out design and optimized solutions. This encompasses minimizing depth of the circuit, minimizing gate errors, and picking optimal qubit mappings to reduce overall noise entanglement.



Noise-aware quantum computing is strongly supported by machine learning technology. Conventional optimization approaches depend on predefined rules and heuristics that cannot necessarily capture the intricate and dynamic quantum noise inherent in a state. In contrast, machine learning provides data-driven techniques that learn patterns from quantum execution data and can adapt to change. Using machine learning models trained on a huge amount of experimental data, we can learn the relationship between circuit configurations and error rates — paving the way to optimized circuits that reduce the effect of noise.

Due to the nature of this kind of problem, one advantage of ML in this case is its ability to generalize also across quantum devices and noise environments. Supervised learning models can learn to predict the fidelity of quantum circuits as a function of their geometry (e.g. scale-dependent dimensions etc.), whereas reinforcement learning agents can iteratively hone circuit designs based on interaction with quantum simulators or hardware stages. Such methods allow for automated and scalable optimization processes going beyond manual tuning, significantly increasing the efficiency of quantum circuit design.

A further [link between quantum computing and machine learning] creates a hybrid computational paradigm by combining the strengths of both technologies. Conventional machine learning models can use big data, parallel processing; quantum systems offer better competitive performance for some problems. Such synergy helps to create smart systems that adapt well to noise and improve as time progresses. Consequently, optimization via machine learning is now an integral part of state-of-the-art quantum computing pipelines.

Noise-aware quantum computing is also significant for its relevance to real-world applications. Most of the quantum algorithms useful for practical applications, such as simulating a chemistry compound or financial modelling, require exceptionally high accuracies—justifying their dependence on QEC—to make sense. These algorithms are sensitive to noise, so it is essential that noise mitigation strategies be included during the circuit design. Using this approach, the researchers trained machine-learning-based solutions that return reliable results in spite of hardware imperfections.

Conclusion Noise-aware quantum computing is an important gateway toward practical quantum systems. To improve the fidelity and performance of quantum computations, one can intelligently design mitigating strategies to deal with challenges arising from noise followed by machine learning-based optimization. In this chapter, we have explained the basic notions about noise for quantum systems and its challenges, that is, given the importance of such issues to combine classical machine learning techniques to tackle these problems more effectively. Noise-aware approaches will be pivotal in moving research from experimental prototypes to real-world applications, as the field of quantum computing continues to change.

Quantifying and Modeling Quantum Noise

One of the main challenges in building a working quantum computing system is associated with quantum noise. In contrast to the classical systems for which errors may often be diagnosed and corrected without extreme difficulty, quantum systems are delicate objects that show great sensitivity to environmental perturbations. To create an optimization framework where we perform machine learning for a hybrid circuit, we need to understand the nature and sources of quantum noise and how do they behave. Here, we develop the characterization and modelling of quantum noise to provide a preliminary for noise-aware optimization in the next chapter.

Therefore, most of the quantum noise is caused by the interactions between qubit and its environment. The interaction leads to DE coherence, where the quantum state loses its coherence over time ultimately leading to a collapse of the superposition state. DE coherence is normally divided into two kinds, amplitude damping and phase damping. Amplitude damping corresponds to the qubit losing energy and transitioning from an excited state to a ground state. In contrast, phase damping modifies the relative phase between quantum states without changing their energy levels. DE coherence of both types widely limits the precision of quantum calculation.

Gate error is the second largest class of noise, arising from deficient implementations of quantum gates. Quantum gates are the primary building blocks of quantum circuits, and small imperfections in their implementations can propagate through multiple operations, resulting in a significant deviation of the direct output. On top of that, measurement errors that happen while reading quantum states due to hardware solutions or interferences, mean the observed value may not be the same as the real state.

Quantum noise needs to be modelled properly so that these errors can be suppressed effectively. Noise modelling is the process of simulating how quantum errors behave using mathematical techniques that can mimic physical reality. For example, in one way of modelling noise (the depolarizing noise model) a qubit has some probability of being replaced by a completely mixed state. It is useful to model random errors in quantum systems. The amplitude damping model is another commonly used one, as it describes the loss of energy in a quantum bit, and thus can be applied to the study of superconducting quantum devices.

As we made progress to bring noise modelling from a modelling-driven approach to a data-driven one, machine learning became an essential tool. Instead of a theory-heavy approach, machine learning algorithms are able to learn directly from experimental data (i.e., noise). As a simple use case, regression models can be used to predict error rates as functions of circuit configurations; neural networks can correlate noise sources with system performance in ways that may be difficult for human beings to devise. Using this data-driven approach permits more accurate and adaptive noise models, which are necessary for optimizing quantum circuits.

In addition to that, one can use Bayesian inference as probabilistic modelling methods which will help estimate the uncertainty in quantum systems. Such methods offer formalism for updating noise models when new data becomes available to keep the system adaptable. This is especially relevant in NISQ devices, as noise patterns can change over time with unstable hardware.

Table 1: Quantum Noise Types

Noise Type	Description	Impact on System
DE coherence	Environment-induced decay of quantum state	Reduces computation accuracy
Gate Errors	Imperfect quantum gate operations	Errors accumulate across circuits
Measurement Errors	Incorrect quantum state readout	Affects output reliability
Depolarizing Noise	Random disturbance of quantum state	Introduces uncertainty
Amplitude Damping	Energy loss in qubits	Alters quantum state evolution

Characterizing noise accurately also allow to develop optimization strategies aware of this noise. Knowing which regions of a circuit are most error-prone allows optimization algorithms to focus on reducing the number of errors in these areas. Within this context, ML models can be trained to detect gates with higher than average errors and propose other gate sequences or configurations that reduce noise effects.

Closing thoughts Quantum noise characterization (or calibration) and modelling is the backbone of noise-aware quantum computation. Hackle, et al. introduced a way of generating more robust models by mixing classical noise approaches (also known as the position space) with machine learning techniques and using them for quantum systems, resulting in a more holistic view on error behaviour [Fig 4]. This is critical to designing an optimized circuit that can continue to function correctly in a weakly controlled noisy environment. New and sophisticated noise modelling approaches will be integral in closing the gap between theoretical promise and practical realisation of quantum computing technologies, as quantum hardware continues to progress.

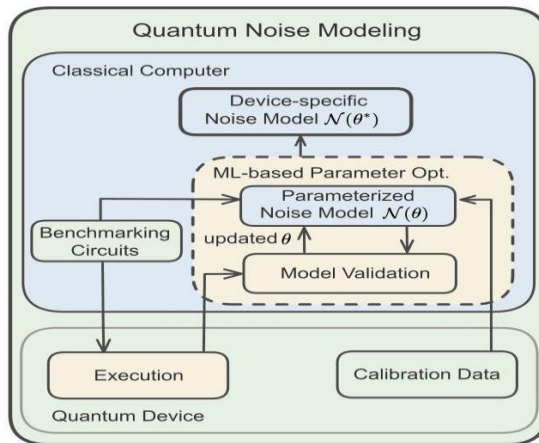


Figure 1: Noisy Quantum Circuit Representation

Characterisation and Modelling Of Quantum Noise

One of the biggest obstacles to creating a fault tolerant architecture for quantum computing systems is the noise introduced by the quantum characteristics of their hardware. While in classical systems it is often straightforward to detect and correct errors, quantum systems are intrinsically fragile and more prone to environmental perturbations. Gaining insights into the source, character and dynamics of quantum noise are therefore critical to develop effective optimization strategies for circuit improvements such as those based on machine learning techniques. It covers the characterization and modelling of quantum noise, creating groundwork for noise-aware optimization in the subsequent chapters in this chapter.

From here on, quantum noise comes mainly from the interaction between qubits and their environment. This interaction triggers the DE coherence process, where the quantum state loses its coherence over time, subsequently collapsing the superposition state. There are two types of DE coherence that we have usually classified: amplitude

damping and phase damping. Amplitude damping is the process of losing energy from a qubit and going from an excited state to a ground state. As for phase damping, it modifies the relative phase between quantum states without changing their energies. Both types place considerable limits on the fidelity of quantum calculations.

Gate error (the second big one) -- any imperfection in the quantum gate operation. Quantum gates are the basic elements of quantum circuits, and even small imperfections in their implementation can accumulate through a sequence of operations to create significant errors at the output. Furthermore, reading quantum states leads to measurement errors, where the measured value can differ from the actual state because of hardware limitations or noises.

Realistically modelling quantum noise is a prerequisite to do this in a practical way. Noise modelling is representing the quantum error behavior (quantum errors) by using mathematical frameworks that simulate real-world conditions. A common scheme is the depolarizing noise model, which reads that a qubit has some probability of being replaced with a completely mixed state. One application of this model is to account for random errors, which occur in quantum systems. One of the most common models is actually the amplitude damping model, with this one simulating energy leaking out from qubits, and naturally suited very well for superconducting quantum devices.

Machine learning is an essential part of generalizing noise modelling to allow data-driven modelling of systems along the quantum scale. Rather than using theoretical models, machine learning algorithms can learn noise signatures obtained directly from experimental data. Regression models may be used to extrapolate error rates given a set of instantiated circuit configurations, while neural networks can learn complicated mappings from noise sources to system performance. This data-intensive method leads to better and more adaptive noise models, which are fundamental in optimal quantum circuit design.

In addition, probabilistic modelling methods, including Bayesian inference may be used to account for uncertainty in quantum systems. These techniques will allow noise models to be updated with new data, keeping the system tuned and adaptable to changes in conditions over time. In particular for NISQ devices, the hardware instability means that noise characteristics can change dramatically over time.

Correct noise characterization additionally makes it possible to formulate noise-aware optimization methods. Knowing what circuits are error-prone allows optimization algorithms to improve the weak links first. For Example, Machine learning models can be trained to recognize high error gates which can recommend alternative gate sequences or configurations in a way that minimizes its impact on noise.

In summary, the characterization and modelling of quantum noise are at the heart of a noise-aware quantum computing. It is able to link traditional noise models with machine learning techniques, providing a more detailed picture of error behaviour for quantum systems. Such knowledge is required for the design of up-relevant circuits working in fact noise situations. With continuing advancements in quantum hardware, sophisticated noise modelling methods provide a vital component towards the realization of the full potential of quantum computing technology.

Where Standard Circuit Optimization Techniques Fall Short

In particular noisy quantum computations, an efficient optimization of quantum circuits is critical to the higher reliability and performance of desired computational tasks up to October 2023. The optimization methods that have been commonly employed include traditional optimization, which simplify quantum circuits, minimize the gate counts and enable efficient execution. As, however, quantum systems become more complicated and operate in a noisy environment, conventional techniques exhibit various drawbacks thereof. This chapter discusses the limitations of traditional circuit optimization techniques and introduces the idea of adaptive-data driven solutions such as machine learning (ML)-based optimizations.

A. Rule-Based Optimization Approaches

Existing quantum circuit optimization is rule-based, with transforms predefined which help to reduce circuits. Such rules comprise for instance gate cancellation, gate merging and equivalent circuit constructions based on established mathematical identities. Synthesis (that is, removing consecutive inverse gates) and rewriting needed neighbouring gate into more-efficient equivalents are well-known techniques.

These methods work well for small-scale circuits, but they are limited in flexibility when applied to more complex or dynamic quantum systems. Rule-based methods are highly reliant on hand-crafted patterns, and do not generalize across hardware noise or circuit structure. Therefore, they may not provide superior solution during practical situations when noise properties are unpredictable and evolve over time.

B. Heuristic Optimization Techniques

Heuristic methods are rule-based solutions with heuristic strategies that move toward better performance on the circuit. These are often referred to as iterative top-down methods or gate reduction techniques, as they follow

the general procedure of iteratively reduce circuit depth and corresponding number of gates by guided search along cost function such as time taken for execution or probability of error. For recommendation methods common heuristic approaches are greedy and local search.

While heuristics are used for faster solutions than exhaustive optimization, they do not necessarily produce the global optimum. They are easily attracted to local minima, which is a common issue for high-dimensional optimisation spaces like in the case of quantum circuits. Two things are clear about heuristic methods, even though they are computationally efficient and relatively simple to implement: they do not take real-time data from the quantum hardware into account (which proves detrimental when noise is present).

C. Lack of Noise Awareness

The lack of noise awareness is one of the most prominent weaknesses of traditional optimization approaches. Widely used classical optimization methods advocate for decreasing circuit complexity without regards to the specific noise profile of the quantum hardware. As a result, circuits optimise to appear simple without coming to fault tolerance, making them very noise tolerance poor.

In fact, a gate sparse circuit could still lead to results with lower fidelity if it scales up the higher error susceptibility gates or targets qubits prone to poorer coherence. Basic methods cannot meaningfully look to reduce error rates or improve circuit fidelity unless noise models are incorporated in the optimisation process. Independent of whether global or local control parameters are to be optimized, the limitations laid out here become especially important in NISQ devices due to the large influence that noise has over system performance.

D. Scalability Challenges

They need their sizes and/or complexities to state-of-the-art classical optimization methods for such cases scale successfully where the size quantum circuits more grow. As the number of qubits and gates increases, exhaustively optimizing a circuit is unfeasible due to an exponential increase in the number of possible configurations. Rule-based and heuristic methods can also be restricted to small or medium-sized circuits, and they may fail in large scale quantum applications.

E. Hardware Dependency Issues

Introduction Quantum hardware platforms show a high degree of variability in the connectivity of qubits, gate fidelity and noise characteristics. Theoretical optimization procedures are frequently based on a simplified or clear (d) assumption of the hardware model and do not account for the real-world restrictions in distinct quantum devices. The inability of these hardware-aware skills often results in an inefficient circuit mapping and higher error rates during execution.

This means that a circuit optimized for, say, one quantum processor might run poorly on another because the qubits are arranged differently, or gates have different performance. Standard optimization methods can't take advantage of modern quantum devices without using knowledge about the hardware.

F. Restricted learning and adaptability

Traditionally, optimisation methods also lack the ability to learn from past experiences. These techniques use neither historical execution data nor react to system performance. Hence, they cannot learn with time or replace when quantum hardware changes its eventual conditions.

On the other hand, machine-learning-based methods can conduct large dataset analysis for pattern recognition and continuously optimize strategies. Because of how traditional methods are static, they do not work well in these types of systems where noise and system behavior evolve over time.

G. Summary of Limitations

To summarize, classical circuit optimization techniques were an essential tool in early quantum computing, but their shortcomings are becoming more apparent for the contemporary noise-sensitive quantum processors. However, their ineptness in adaptability, scalability and noise-awareness limits their applications to the real-world scenarios. Intelligent optimization solutions are required that leverage data, adapt to the hardware conditions and become better with experience. To address these limitations, research focused on approaches based on machine learning may be a promising route to more efficient and reliable quantum circuit optimization down the line.

Quantum Optimization Foundations In Machine Learningchapter

Combining machine learning (ML) and quantum computing can provide new approaches for one of the biggest problems in quantum circuit optimization — reducing noise. Machine learning offers adaptive, data-driven approaches that can learn complex patterns and driving strategies from existing data. More specifically, by virtue of their inherent ML techniques are now frequently used in quantum computing to optimize circuit structures, predict noise behavior and enhance overall system efficiencies. In this chapter, we give the machine-learning concepts that set the ground for quantum optimization and their importance and applicability in noise-aware quantum systems.

A. A Short Introduction to Machine Learning Paradigms

There are multiple paradigms of machine learning because each paradigm is good for a different type of problem. Machine learning uses a supervision method with three main types of ways; they are supervised learning, unsupervised learning and reinforcement learning. In supervised learning, the model you train gets from labelled data where input-output match is certain. As an example, in the case of quantum optimization, its use may be to predict circuit fidelity or error rates based on certain configurations. Meanwhile, unsupervised learning works with unlabelled data, and just finds hidden patterns/structures in the datasets. This approach is beneficial to cluster similar noise patterns or identify anomalies in quantum systems. Reinforcement Learning (RL) is an agent that interacts with the environment and updates its actions based on rewards or penalties. For instance, RL has shown great promise in optimizing quantum circuits by having gate sequences and circuit layouts improve with each iteration.

B. Relevance between quantum systems and feature representation

One important question in using machine learning for quantum optimization is the way that quantum circuit data is represented for use with ML models. Quantum circuits are described as sequences of gates, connections between qubits and measurement outcomes. All these need to be transformed into numerical features that can work with machine learning algorithms. For gate sequences: Common approaches include using vector representation, where the dimension of vectors indicates a gate used from one time to the other (e.g., x possible gates) and adding two dense layers to define an edge (weight); For both circuit depth and qubit connectivity: circuit depth typically represents how many iterations or levels of operations need to be applied for computation, therefore can either be represented as numerical values or by means of state labels as illustrated in Fig. 4A; based on classical machine learning techniques it could also help if we provide compute layer structures that represent which parameter you are currently working with while using adjacency matrices to describe qubit connectivity enabling software chips compatible systems.

In turn, feature engineering is extremely important as it makes the sure that the ML model retains most relevant information of the quantum system. For instance, parameters such as gate fidelity, qubit coherence time and error rates can have a major impact during the optimization process. Selecting and preprocessing these features enables a machine learning model to be more accurate and generalize better.

C. Error prediction through supervised learning

In quantum circuit optimization, supervised learning is popular for predicting errors and performance metrics [1]. For example, linear regression, decision trees, and indeed neural networks can be trained on historical data of error rates inferred from measuring the output of several runs of different quantum circuits to predict an upper bound on this same measure for new circuit configurations. This enables the optimization algorithms to pick circuit designs that have lower noise and improved fidelity.

More precisely, deep learning models like feed forward neural networks are capable to model non-linear relations between circuit parameters and performance metrics. These models are capable of learning complex dependencies by training on large datasets and thus can be generalizable even to highly noisy environments. Such a feature is necessary for real-world quantum devices that require circuit optimization.

D. Unsupervised Learning to Find Patterns

Explore the structure of quantum data — Unsupervised learning techniques are data agnostic as they do not require label dataset. However, clustering algorithms (e.g., K-means or hierarchical clustering) can classify similar circuit configurations with respect to the noise characteristics. It enables the recognition of patterns and trends that may not be apparent through manual analysis.

Techniques for dimensionality reduction, such as Principal Component Analysis (PCA), are also employed to As well simplify high-dimensional quantum data while retaining significant information. This allows handling more complex datasets and process, visualizing and optimizing quantum circuits in a more efficient way.

E. Adaptive Optimization with Reinforcement Learning

Reinforcement learning (RL) has been one of the most promising methods for quantum circuit optimization. Within this framework, an agent interacts with a quantum environment, taking actions like choosing gate series or changing the circuit structure. The agent is trained on rewards based on the success/failure of the circuit, for example in terms of error rates or lower reduced fidelity.

In the long run, the RL agent learns to maximize rewards by finding better strategies for circuit design over time! It includes algorithms such as Q-learning and policy gradient methods. RL is inherently robust, dynamic and well fitted for the variations and uncertainties that quantum systems exhibit.

In practice, ML models are often embedded within hybrid quantum–classical systems [3]. Here, traditional ML algorithms evaluate data and formulate optimization plans, while optimized circuits run on quantum processors. This repetitive process forms a feedback loop in which the system is constantly getting better dependent on how well it performs.

Although machine learning has many advantages, using it for quantum optimization still holds significant challenges. As a case in point, there is not enough high-quality quantum data available, and this can restrict the model training processes. Moreover, training of complex ML models itself may be computationally expensive when dealing with large quantum systems.

The second challenge is that the ML models needs to generalize across different quantum devices and noise. In general, optimization strategies can be ineffective in the real world if you over fit to particular datasets. Overcoming these obstacles necessitates thoughtful model design, data augmentation techniques, and on-going validation.

Milwaukee, WI–Finally, machine learning benefits from having a strong basis to minimize quantum circuits and denies quantum devices. Accordingly, employing supervised, unsupervised and reinforcement learning methods allows one to create adaptive and efficient optimization strategies that exceed traditional ones. This combination of ML and quantum computing brings us closer to the development of reliable, practical quantum systems. Such techniques will continue to become more important for practical quantum computing as the science advances.

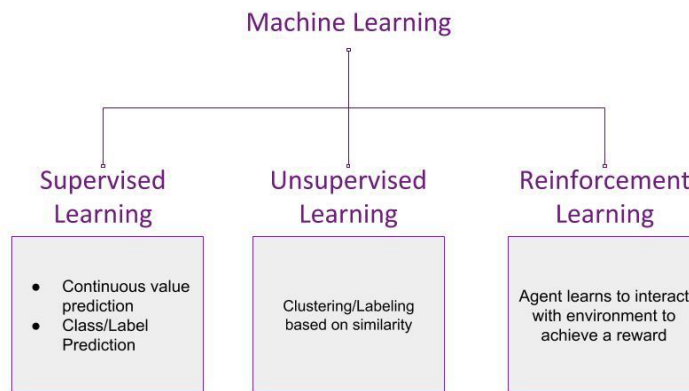


Figure 2: Machine Learning Paradigms (Supervised, Unsupervised, RL)

Data-Driven Noise Prediction Models

Understanding and suppressing noise in quantum circuits is a central challenge of quantum computation, especially given the rapid development of devices over the past few years. Quantum devices are more susceptible to noise than classical systems, adding noise prediction as a prerequisite for reliable computation. For example, traditional analytical models can offer an elementary perspective on noise behavior; however, they may not encompass the complexity and variability seen in actual quantum hardware. Machine learning-based data-driven noise prediction models have emerged as a strong alternative to overcome this shortcoming. The former cause these models to learn patterns of noise and error behavior based on historical quantum execution data, which helps inform more adaptive and efficient circuit optimization.

Data-driven approaches: These are based on the availability of datasets generated from quantum experiments or simulations. Such datasets generally consist of circuit configurations, sequences of gates, which quits were directly interacting with each other, conditions under which execution is done and error rates they observed. Machine learning models can learn relationships between circuit parameters and noise characteristics by examining this data. These discussions help in developing predictive models that provide an estimate of error probabilities prior to circuit execution. These predictions are important for optimizing the design of circuits because once these configurations are known, configurations can be selected that minimize noise impact and enhance overall fidelity.

Regression modelling is a very commonly used technique for data-driven noise prediction. Continuous valued estimations like error rates or circuit fidelity can be broken down into standard regression models such as linear regression, polynomial regression and support vector regression. These models are trained on labelled datasets that encode the electrical features of circuits as input features, while the total noise present in the circuit is reflected in an output label. The simple regression models are easy to construct and interpret, howbeit they might fail to

retrieve (learn) the complex nonlinearity of quantum systems. Wider and deeper neural networks are usually used to train deeper models than this limit (train deep models).

Deep learning models, namely neural networks, have been demonstrated to work well for predicting quantum noise. Deep learning models are based on multi-layered interconnected nodes, and can discover complex patterns in large datasets. As a result, although neural networks are trained on very simple quantum circuit data, because they can learn extremely complicated mappings from inputs to outputs, using data that is quite diverse can help them encode more complex dependencies between the structure of a given circuit and how noise behaves when it runs. A deep neural network, for example, can learn how specific gate sequences or qubit interactions lead to higher error rates facilitating better predictions than the traditional methods. Moreover, convolutional neural networks (CNNs) are suited for experimentation with quantum circuit classification and analysis of structured representations of unitary gate operations [5], while recurrent neural networks (RNNs) can accurately model sequential gate execution.

Probabilistic modelling is another key approach for noise prediction. Bayesian inference and Gaussian processes are examples of techniques that offer the tools to model uncertainty in quantum systems. Not only do these methods predict the levels of noise, but they also quantify the degree of confidence in those predictions, which is critical for making more informed decisions within optimization processes. Probabilistic models are useful when there is little or noisy data, since they are able to incorporate prior knowledge and update predictions as new data arrive. This makes them particularly promising for dynamic quantum environments, where the noise characteristics evolve in time.

In essence, one might formulate the noise prediction process as a sequential decision making-type of problem, so reinforcement learning could be used here too. Specifically, an agent learns to predict and reduce noise by communicating with a quantum environment and receiving feedback based on the prediction. As time progresses, the agent learn to predict better, resulting in improved optimization strategies. This strategy is especially beneficial in adaptive systems that need to learn over time.

One of the main strengths of data-driven noise prediction models is that they can generalize across many different quantum devices and configurations. Training on heterogeneous datasets, these models can learn device-agnostic features that are transferable across devices. This is especially pertinent in the current stage of quantum computing development, where different technologies such as superconducting qubits, trapped ions and photonic systems have very different noise characteristics. An inference model can learn to overcome these differences and gain consistent performance in different platforms.

Table 2: Effectiveness of Data-Driven Noise Prediction Models

Model Type	Application	Advantages
Regression Models	Error rate prediction	Simple, interpretable, easy to implement
Neural Networks	Complex pattern recognition	High accuracy, flexible, captures non-linearity
Probabilistic Models	Uncertainty estimation	Handles noisy data, works with limited datasets
Reinforcement Learning	Adaptive prediction	Continuous improvement, dynamic learning

While data-driven models have their advantages, they are also not without challenges. A significant problem is the lack of good quantum data, limiting running a good model. For one, training complex models requires a lot of computational power which is not always at hand. One of the three main challenges is generalizability across different hardware and possibly noisy testing conditions. To tackle these challenges, we need to create effective data gathering approaches, scalable training mechanisms, and solid validation paradigms.

Thus, as a whole, data-driven noise prediction models mark a new chapter in quantum circuit optimization. These approaches utilize machine learning techniques to gain more accurate and adaptive understanding and characterization of quantum noise. The fact that they learn from data, generalize across systems and continuously improve them, makes them fundamental to modern quantum computing workflows. Data-driven approaches will be key for establishing reliable and scalable quantum computing systems as research in this area continues to progress.

Reinforcement Learning for Adaptive Circuit Design

Reinforcement learning (RL) has become a very strong method to optimize quantum circuits, especially in dealing with the noise present in many quantum systems. However, in mechatronics and robotics systems, where labelled datasets may not be readily available, reinforcement learning teaches a system the best paths to take for reward through its interactions with an environment in which it operates—it does not require pre-labelled datasets like traditional machine learning techniques would. This environment can be a quantum simulator or real-world quantum hardware and the learning agent continues to change circuit configurations until it gets an improved result. Reinforcement learning in this context serves its ultimate goal: to consistently optimize decision-making from feedback, achieving minimized noise and maximal circuit fidelity.

Systems of reinforcement learning based quantum optimization runs in a cycle of observation, action and reward. The agent sees a state of the quantum circuit which can be the gate sequences, qubit connections, error rates etc. Considering this state, the agent chooses an action such as the modification of a gate or ordering of operations that can affect the overall depth of circuit. Once the action is performed, we evaluate the result and return a reward for how good that change was. This reward is often given depending on performance measures, e.g. lowering the errors, enhancing fidelity, less complexity of circuits. As it matures, the agent learns which moves result in greater success and fine-tunes its game plan.

One of the primary strengths of reinforcement learning lies in its exploration capabilities in intricate and high-dimensional solution spaces. Quantum circuits can be composed of a number of parameters, and finding the optimum configuration is not feasible using traditional optimization methods due to an enormous state space. This is where reinforcement learning tackles this challenge and gets the right amount of exploration versus exploitation. Exploration enables the agent to experiment with new circuit configurations and find better solutions while exploitation concentrates on improving already helpful configurations. This balance allows the system to quickly look through circuit topologies that reduce noise and increase robustness.

Reinforcement learning also provides adaptability — particularly important since the noise characteristics of a quantum environment can change over time. In contrast to static optimization methods, reinforcement learning models are continually improved with new data and feedback. That makes them particularly useful for real-time optimization, where the learning system must adapt to changes in the hardware performance or environmental conditions. This is why reinforcement learning can offer more advanced and adaptable solutions than traditional methods.

The design of the reward function is another key point of reinforcement learning in quantum circuit optimization. Closest to learning, the reward function comes into play: it tells the learner (or agent) how to perceive its actions. The reward function needs to encompass various targets like the noise constraints and circuit depth, as well as correct computation. Finding the right balance between these objectives is therefore difficult but crucial to guarantee that agent learns for complex and effective optimization.

While this has its advantages, reinforcement learning with quantum systems does have some disadvantages. Nature of the Work Reinforcement learning models can be expensive to train, especially for circuits that are large or environments that are complex. Furthermore, the intrinsic randomness associated with quantum systems can lead to high variability in the reward signals, making it challenging for the agent to learn consistent patterns. Researchers overcome this challenge by using quantum simulators for initial training, but then transfer the trained models to real quantum hardware. This hybrid technique enables to reduce computational cost while keeping the predictive and practical relevance.

So summing up, reinforcement learning is a great approach to designing and optimizing quantum circuits with noise. It learns through interaction and fine-tunes its strategies that allow for more efficient exploration of circuit configurations for the elements of interest to performance in a noisy environment. While quantum computing technology continues to evolve, it is predicted that reinforcement learning will be a key element for the creation of intelligent optimization methods aimed at improving both the reliability and scalability of these systems.

Optimizing a Quantum Gate Using Deep Learning

Machine Learning has now evolved into a powerful extension of itself known as Deep learning that can model very complex and non-linear relationships in data. Indeed, with the advent of quantum technologies such as quantum computing, deep learning methods are used to optimise the gates and structures of a circuit to achieve minimal noise and higher computational accuracy. Quantum gates or basic operations acting over a single qubit or pairs of qubits perform the logical actions and any error encountered during its operation may affect the fidelity for quantum computations. Gate operations are frequently subject to errors because of hardware imperfections and environmental disturbances. Deep learning enables data-driven insight guiding the exploration of these errors and determining gate configurations for improved performance.

There is a vast literature which uses deep neural networks (DNNs) to model the mapping between quantum circuit parameters and performance metrics, such as fidelity and error rates. They comprise several hidden layers which allow them to learn hierarchical representations of data. DNNs can be trained on data sets that have information about a gate sequence, qubit interactions and characteristics of noise for quantum gate optimization. The model can predict the effect of unique gate configurations on circuit quality and propose alternatives accordingly, after being trained.

CNNs are especially applicable in cases where quantum circuits can be disclosed in structured forms like matrices or grids. CNNs can recognise spatial patterns of gate arrangements, and can expose dependencies among neighbouring qubits. Likewise, RNNs are powerful for sequential modelling and can be used to analyze any quantum

circuit containing time-ordered gate operations. These models may maintain dependencies over sequences of gates, and as such, provide information on how early operations affect subsequent outcomes.

One of the primary advantages delves into deep learning, where it can learn features directly from the raw data without having to engineer them manually. For quantum gate optimization, this allows the model to learn key features of gate operations — e.g. error-prone configurations or inefficient sequences — without hard-coded programming. Deep learning models learn these features and can improve predictions & optimization strategies.

Various approaches using this activation function focus on feature representation in quantum systems which involve encoding of the circuit parameters into several numerical representations that can be processed (Passed as inputs) by the neural networks. These could be the types of gate, rotation angle, qubit index, and any patterns or trace that determines connection or circuit. Basically, feature representation quality is instrumental to guarantee deep learning model effectiveness as it translates into the amount of relevant information that models are able to capture. Gate sequence optimization is a common use case of deep learning in quantum computing. A more complex collection of inclusive quantum gate sequences may lead to longer circuit depth, which exposes the qubits to noise for a longer duration hence leading to a greater error rates. Based on the already learned gate sequences, DL models can also examine noise impacts and bring simplification or reordering opportunities.

E.g. a neural network trained within the framework can recommend a different sequence of gates that performs the same computation while using fewer operations or having a lower probability of error. Doing this not only makes the circuit effective but as well boosts speed of a SY stem. Moreover, deep learning may allow a gate sequence to control the execution on new hardware architecture, thus optimizing it. Deep learning models can inject noise information within the training loop itself, making it easier to design noise-aware gates. When a model is trained on designed data sets that have noise properties of real experiments, it learns through the training objective which gates or gates sequences are more fragile? It enables the system to favour configurations with least bit of noise exposure.

In the context of NISQ devices, where error rates differ from qubit to qubit and operation to operation, noise-aware optimization is especially crucial. Deep learning models can effectively account for heterogeneity in hardware platforms and provide tailored optimization strategies. This inherent adaptability renders deep learning a useful weapon in the armoury increasingly being created to enhance the reliability of quantum computations. Gate optimization based on deep learning methods is mostly run within hybrid quantum-classical frameworks. So, the classical deep learning models evaluate the circuit data and propose optimization strategies, which are then executed on the quantum processors. This feedback loop builds an iterative process where performance undergoes continuous improvement based on real-time outcomes.

With deep learning and quantum computing, we can combine scalability and automation for the optimization processes in such a way that we do not require near manual processes anymore. This also enables real-time tuning, allowing the system to adjust rapidly to changing conditions and continue performing at a high level. However, deploying deep learning for quantum gate optimisation brings a number of challenges. A key hurdle is the supply of high-quality data for training, because quantum experiments can be expensive and prolonged. Deep learning models, on the other hand, needs a lot of computational power for training which can limit their usability.

Ensuring that the models generalise to different quantum devices and noise conditions is another challenge. Optimization strategy may be limited by over fitting to chosen datasets in real world applications. To tackle these challenges, careful model design, various data augmentation techniques and continuous validations are some of the key areas.

To summarize, deep learning enables to optimize quantum gates and boost circuit performance in the presence of noise. Utilization of advanced neural network architectures can also allow the complex relation between gate configurations and noise to be captured, stirring more effective optimization techniques. The advancement of quantum computing is only a matter of time and deep learning is one prime aspect driving to facilitate the rapid progress with the combination of features extracted via artificial intelligence, adaptability to different conditions and integration into hybrid systems. As research works its way forward, deep learning may become an even more potent vehicle for building modular and scalable quantum technologies that are efficient and reliable.

Hybrid Quantum-Classical Optimization Frameworks

A. Introduction to Hybrid Frameworks

Hybrid quantum-classical optimization frameworks are a practical and powerful means of enhancing the performance of quantum circuits in the current era of noisy quantum hardware. However, hybrid systems leverage the strength of classical computing combined with quantum processing to attain better results, as fully fault-tolerant quantum computers are not expected for some time. Within these frameworks classical algorithms perform tasks

such as data analysis, optimization and learning; whilst quantum processors run circuits and output computations. By combining many datasets, researchers can bypass hardware limitations and derive noise-reduction techniques.

B. Architecture of Hybrid Systems

A standard hybrid quantum–classical architecture can be always decomposed into three high-level pieces: a classical optimization engine, a quantum execution unit and a feedback loop. The classical part analyses circuit performance suggests optimization strategies based on the performances and updates parameters observed from the results. The quantum part runs circuits on simulators or real quantum devices and returns measurement results representing how the system works.

This feedback loop joins these components by transmitting information between them. The classical system then receives the results after each quantum execution, and measures certain performance characteristics like fidelity, or error rates. Following this assessment, the classical optimizer varies circuit parameters and sends them back to the quantum processor. It repeats this process iteratively until converging to an optimal or nearly-optimal solution.

C. Machine learning in hybrid optimization

Central to hybrid frameworks is the time-domain machine learning, which facilitates an intelligent and adaptive optimization. Classical ML models then study huge datasets derived from quantum executions and score the patterns that can be used to aid circuit design. Supervised learning models can predict how well different circuit configurations behave, while reinforcement learning agents learn and iterate on the optimization process, usually through trial and error.

This process is further improved by deep learning models, which can learn more complex relationships between circuit parameters and their noise behavior. These models can provide recommendations on the ideal sequences of gates, optimal mapping of qubits to physical devices or the circuit structure itself such that noise is reduced and efficiency increased. The incorporation of machine learning into the hybrid framework enhances its addictiveness and allows it to operate in a single-shot manner for dynamic quantum systems.

D. Variational Quantum Algorithms

Key ingredients of hybrid quantum–classical frameworks are the so-called Variational quantum algorithms (VQAs). These algorithms utilize parameterized quantum circuits, where the parameters for particular gates are updated iteratively to optimize a specific objective function. Classical algorithms perform the optimization, updating the parameters based on measurement results from the quantum circuit.

Because they efficiently learn characteristics that are specific to the hardware at the time of capture, VQAs are particularly good at demonising. VQAs enhance circuit fidelity and reduce error rates by tuning circuit parameters as informed by observed noise patterns. VQAs could be exemplified by the Variational Quantum Eigen solver (VQE) and Quantum Approximate Optimization Algorithm (QAOA), which successfully prove its potential on the applications.

E. Benefits of Hybrid Optimization

Roughly speaking, hybrid quantum–classical frameworks hold certain benefits over the classical or quantum methodology only. A major advantage is computational presumability: the classical systems operate on optimization tasks that consume a lot of resources, while quantum processors focus on executing ever more circuits. This division of labour reduces the total computation involved and thus speeds up optimization.

Another advantage is adaptability. In dynamic and noisy environments, hybrid systems are well-suited as they update their learning incrementally on new data and adjust their strategies accordingly. Moreover, such frameworks can also be scaled to accommodate more complex quantum circuits as technology advances.

F. Practical Implementation Considerations

Several factors have to be thought of when implementing hybrid optimization frameworks. Not only do classical and quantum components need to communicate, but that communication needs to be quick to reduce latency and ensure things move smoothly. Similarly, we also need to optimize the encoding and decoding processes so that as little overhead is incurred.

Quantum hardware compatibility is another essential aspect to consider, since different quantum devices have distinct features and limitations. Hybrid frameworks should be equipped to handle these variations and deliver consistent performance across platforms. In addition, error mitigation approaches need to be incorporated into the system in order to improve fidelity.

G. Challenges in Hybrid Frameworks

Hybrid quantum–classical frameworks have their own advantages; however, they are faced with several issues. Latency due to communication overhead between classical and quantum systems is an important problem, especially when it comes to cloud-based quantum processors. This can reduce the speed of optimization and limit real-time execution performance.

The reliability of feedback is not be reliable because of noise in quantum hardware, thus another challenge arises in the accuracy of measurement results. The complexity of the machine learning models specially designed for quantum systems also may increase the computational cost as well as difficulty in overall implementation. These challenges are increasingly solved through hardware and software technology.

H. Conclusion

In summary, one of the most effective features for mitigating quantum circuit noise is hybrid quantum–classical optimizations. These frameworks deploy joint but selective advantages of classical machine learning and quantum computation towards adaptive, scalable and efficient optimization tactics. By incorporating feedback mechanisms and utilizing Variational algorithms, they become even more adept in managing complex and dynamic environments. Hybrid frameworks will become an important part of the quantum technology growth curve as they help connect today and tomorrow.

Noise-Aware Qubit Mapping and Routing

Noise-aware qubit mapping and routing are of paramount importance for the performance and reliability of quantum circuits, especially in Noisy Intermediate Scale Quantum (NISQ) devices. Qubit mapping is the process of assigning logical qubits in a quantum algorithm to physical qubits on a quantum processor. On the other hand, routing is determining how qubits gates interact with one another using quantum if we do not have direct connections between them. Due to the limited connectivity of quantum hardware and differences in qubit noise characteristics, anything other than efficient mapping and routing can drastically raise errors and lower the performance of circuits. It follows that these processes need to be optimised in terms of reducing noise in order to make quantum computations precise and reproducible.

Qubit Mapping is usually performed in traditional methods by static or heuristic techniques without rigorous analysis of noise characteristics of the hardware. Often, such methods seek to reduce the expansion in the number of extra operations (e.g. SWAP gates) needed to implement a circuit. But they ignore how error rates for different qubits and connections will differ. This implies that a gate count–optimal mapping may still be poor in practice (high noise). This limitation can be mitigated by adaptive qubit mapping, commonly known as noise-aware qubit mapping, which provides knowledge of hardware-specific noise and integrates it into the mapping process, assigning logical qubits to its 'best' physical qubits.

The power of data-driven decision-making has enabled machine learning techniques to significantly advance noise-aware mapping. Machine learning models can detect trends in the performance of qubits by examining execution history data and correlate them with the relative reliability of qubits for certain operations. These models could also consider the effect that different mapping strategies can have on circuit fidelity enabling the system to prefer parameter configurations with lower noise characteristics. Supervised learning models may be trained to predict error rates on qubit assignments, whereas reinforcement learning agents are capable of exploring a space of mapping strategies and discovering optimal policies through interaction with the quantum environment.

Routing is also significant for the execution of quantum circuits, as it influences noise directly. Most quantum processors have limited qubit connectivity so it is common for extra operations to be needed to route the connections between distant qubits. This subjective operation, for example SWAP gates, adds circuit depth and increases qubit noise exposure time. While, noise-aware routing is interested in reducing the number of such operations and at the same time considering how reliable are the used connections. Using lower-error qubits and gates, one can reduce the effect of noise on the circuit by choosing routing paths that favour more critical and well-performing parts of the device.

The role of deep learning models in better routing strategies is a success story. These models are capable of examining the same complicated connective graphs and determining ideal routes for qubit interactions. Deep learning techniques can produce routing solutions that are efficient yet reliable by taking into account both structural and noise factors. GNNs are also used to model quantum hardware like graphs for more realistic modelling of the connectivity and noise distributions across qubits. This enables more advanced optimization methods that consider the full complexity of the quantum system.

Noise-aware mapping and routing also has the advantage of scalability to various hardware architecture. Different quantum devices have diverse qubit configurations, connectivity and noise properties. Because of these variations, machine learning-based approaches may generalize across them by training device specific patterns and

optimizing strategies based on that. This adaptability will be paramount with the endless stream of new quantum technologies coming on line, all with their particular hardware limitations and performance profiles.

However, many challenges still exist to implement effective noise-aware mapping and routing techniques. A significant problem is the computational cost of the optimization process, where the number of available mappings and routes experiences an exponential growth in terms of the amount of qubits. This means that for large-scale systems it can become hard to see optimal solutions. Moreover, the nature of the quantum noise is dynamic: models must be updated over time to remain true and this requires continuous sampling and retraining of data.

Noise-aware qubit mapping and routing are mandatory for state-of-the-art quantum circuit optimization. Introducing information about the noise of a particular type of hardware, these methods use machine learning to speed up circuit fidelity and reduce error rates. They will be versatile across different devices and can adapt through iterative optimization cycles, making them an excellent driver for the development of quantum computing. With continued research, advances in the algorithms and integration with hardware will make noise-aware optimization even more productive and help us achieve practical reliable quantum systems.

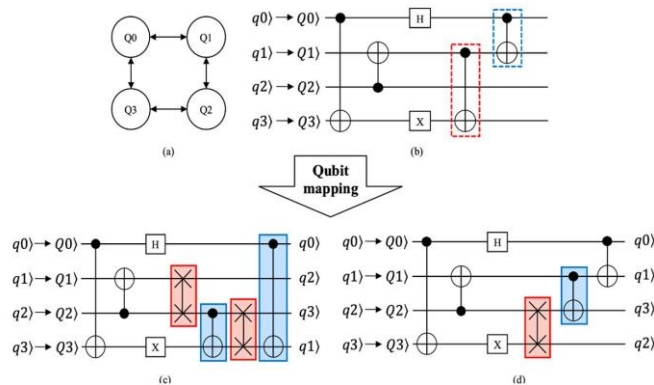


Figure 3: Qubit Mapping on Quantum Hardware (Logical → Physical)

Future Directions and Conclusion

MACHINES: training on data until October 2023 then using machine learning to support quantum circuit optimizations, mainly for noise which is one of the main challenges for quantum computing. Given the DE coherence, not-perfect gate operation and environmental disturbance current quantum systems must be strictly hardware limited and these errors are a fundamental limit of computing Convex659. Such limitations render quantum computing only usable in the noisy intermediate-scale quantum (NISQ) setting, where obtaining large numbers of accurate and reproducible results remains a major challenge. Machine learning based techniques have shown significant potential to mitigate these issues through adaptive and data-driven optimization strategies. In this way, historical execution information can help inform every bottleneck their circuit will indubitably face in future stabilities and permit a machine learning model to dynamically optimize the design of the \mathcal{U} coral circuit and execution based on patterns learned in noise behavior. Although this is still preliminary work for this domain, several promising directions in research are forming that may shape our quest towards quantum computing with inherent noise resilience [25].

One crucial direction for the future is the creation of completely autonomous quantum compilers. Dedicated next-gen systems aim to provide full automation of the design, optimization and execution of quantum circuits through cutting-edge machine learning models. Static compilers at this moment of time still rely on set rules to optimize code and you have to manually tune these manuals; build a new optimized compiler every time when you want a new optimization for your project. While autonomous priced compilers measures execution data itself and it keeps learning as they run over time. These systems output circuits tailored for a given quantum device, while adapting to varying hardware features and noise properties. This means more efficient use of computation and the quantum program becomes scalable. This can therefore lead to self-governing or autonomous quantum compilers which have the potential to democratise quantum processing, allowing researchers and developers — without a background/hardware in quantum physics — access technologies.

The evolution of quantum hardware is also essential. In any case, the error rates for quantum computation of any kind are many orders of magnitude too high in order to be useful and sufficient methods (that scale) do not exist yet. Improving qubit design, error correction codes and hardware stability would take precedence. Another aspect in accompaniment role of the machine learning techniques is also to cut down route considering magnetic string test points to be corrected and warn us regarding how: use as effectively as possible the available hardware resources. On the other hand, predictive models may be used to learn error sequences and calibrate circuit wide configurations

dynamically, enabling improved system level performance. With the commensurate advances in hardware and smart optimization algorithms, this shift from lab demonstrations of quantum devices to practical, scalable implementations of real-world applications will accelerate.

Another massively important aspect of development in the future is very much hybrid quantum–classical systems. Such systems benefit from the capabilities of both classical and quantum processors, yielding in a system that can optimize a quantum circuit as well as run it optimally. Hybrid frameworks leverage classical ML models to analyze data, select the parameters of quantum computations—and depending on a cost function (which can be as trivial as fidelity), even optimize these parameters—while quantum processors perform some extreme demanding operations using different types of desirable effects powered by quantum parallelism. The more intelligent the models and algorithms undergirding your machine learning, the increasingly complex optimization problems they can solve, assisting you in developing even better hybrid systems. Whatever the advantages of quantum technology, its beneficial implementation would depend on an effective interaction with classical approaches and systems—something that across industries from health to finance or scientific advancement must happen in order to resolve significant large-scale challenges experts emphasized will be critical as key enabler to scale quantum applications.

Using modern deep learning architectures to assist in quantum circuit optimization is one of the most emerging directions within this space. QR: Quantum square going for different kind of classical machine learning model — Clonal neural networks, recurrent neural networks and transformer architectures This is a good justification to treat those models as an analytical for both quantum circuits and behaviour of noise, since these models can capture complex patterns and dependencies in data. For example training a deep learning model to predict outcome of qubit gate sequences on performance or searching optimal mappings/restacking that reduce error rates. Moreover, because quantum hardware can be represented as networks of coupled systems², complex interactions and connectivity constraints between the different qubits would better be described using graph neural networks³⁷. Such approaches could lead to a significant improvement in the speed and accuracy of quantum circuit optimization.

Going forward, data quantity and quality will also be a key ingredient in machine learning–based quantum optimization. More quantum experiments will be performed, enabling larger and more diverse collections of datasets to be harnessed, leading to dynamically building ever-more-complex and robust models. Partnerships between academia and industry as well as partnerships with research organizations to create shared datasets and common benchmarks should also take place. With those tools one could learn many optimization methods in a comparative way [14] and accelerate the development of this field. Or, so as to reduce the number of training data required; transfer learning and federated learning may be used in which knowledge from other quantum systems is leveraged.

Despite these encouraging advances however, much work is still needed. The statistical nature of quantum hardware, the size and evolution cost of training those models, and the fact that we need to do this all in real-time remain formidable problems. Additionally, it is necessary to validate the generalization of optimization strategies across heterogeneous devices and conditions to support widespread use. These challenges require long-term, concerted interdisciplinary investigations across quantum physicists, computer scientists and artificial intelligence.

The abstract Quantum computing is a developing field that has the potential to change minds ranging from cryptography to optimization, but the realization of such capacities demands an efficient implementation of quantum circuits. Using machine learning, a new and powerful approach, to optimize these systems; Adaptive, intelligent and efficient optimization strategies are helping machine learning solve one of the most prominent problems facing us ever since the advent of quantum systems. As hardware, algorithms and the data available to be processed become ever more developed over time, these approaches will facilitate broadly scalable, reliable and high-performance quantum technologies. This combination of machine learning and quantum mechanics will create a new frontier in quantum computing that could spur innovations across science, engineering and industry.

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